

HM\_0 cut #1 side 1,  $d = 2$ : this  $H_2$  face has  $H_1$  edges from 3 different  $H_1$  faces adjacent (planar embedding from Sage;  $H_2$  face shown in orange;  $H_1$  edges grouped by face)

